

Performance comparison of lithium-niobate-based extremely high-field single-cycle terahertz sources [Invited]

György Tóth¹, László Pálfalvi¹, Szabolcs Turnár¹, Zoltán Tibai¹, Gábor Almási^{1,2}, and János Hebling^{1,2,3*}

¹Institute of Physics, University of Pécs, Pécs 7624, Hungary

²Szentagothai Research Centre, University of Pécs, Pécs 7624, Hungary

³MTA-PTE High-Field Terahertz Research Group, Pécs 7624, Hungary

*Corresponding author: hebling@fizika.ttk.pte.hu

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Tilted-pulse-front-pumping (TPFP) lithium-niobate terahertz (THz) pulse sources are widely used in pump-probe and control experiments since they can generate broadband THz pulses with tens of microjoules of energy. However, the conventional TPFP setup suffers from limitations, hindering the generation of THz pulses with peak electric field strength over 1 MV/cm. Recently, a few setups were suggested to mitigate or even eliminate these limitations. In this paper, we shortly review the setups that are suitable for the generation of single-cycle THz pulses with up to a few tens of megavolts/centimeter focused electric field strength. The THz pulses available with the new layouts pave the way for previously unattainable applications that require extremely high electric field strength and pulse energy in the multi-millijoule range.

Keywords: terahertz pulse generation; nonlinear optics; ultrafast optics.

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1. Introduction

Nonlinear terahertz (THz) science started about two decades ago, when high-field THz pulses with frequencies of several tens of THz were generated in a GaSe semiconductor and were used as a pump pulse in pump-probe measurements^[1]. THz pump-probe measurement on the sub-THz to few-THz range became first possible, to the best of our knowledge, with the use of a lithium-niobate (LN) THz source pumped by near-IR ultrashort laser pulses in 2010^[2]. Since LN has more than two times higher index of refraction in the THz range than in the near-IR range, tilted-pulse-front pumping (TPFP) is needed in order to achieve velocity matching for the optical rectification process in LN THz sources^[3]. The velocity matching condition reads as

$$v_v^{\text{gr}} \cdot \cos \gamma = v_{\text{THz}}^{\text{ph}}, \quad \text{or} \quad n_{\text{THz}}^{\text{ph}} \cos \gamma = n_p^{\text{gr}} \quad (1)$$

in the TPFP THz pulse generation setups, where v_p^{gr} and n_p^{gr} are the group velocity and group index of refraction of the pump pulse, $v_{\text{THz}}^{\text{ph}}$ and $n_{\text{THz}}^{\text{ph}}$ are the phase velocity and (phase) index of refraction of the THz pulse, respectively, and γ is the necessary pulse-front-tilt angle, which is 63° for LN. The conventional TPFP THz source [see Fig. 1(a)] contains three main optical elements: (1) an optical grating to introduce a pulse front tilt, (2) a lens or an optical telescope to image the tilted pulse into the LN

nonlinear optical material (NM), and (3) an LN crystal. The LN has to be prism-shaped with a wedge angle of γ in order to make possible perpendicular in-coupling of the pump laser and out-coupling of the generated THz beam. (The THz beam generated inside the LN propagates at an angle γ with respect to the propagation direction of the pump beam.) This conventional TPFP LN THz source has become very popular and widely used in THz pump-probe measurements and in experiments controlling material excitations^[4]. In these cases, the typical THz pulse energy, focused THz field strength, and pump spot size are of a few microjoules (μJ), a few hundreds of kilovolts (kV)/centimeters (cm), and a few millimeters (mm), respectively.

Many possible applications of THz pulses have been proposed^[5–11] and demonstrated^[12–19], which need the application of THz pulses with significantly above 1 MV/cm peak electric field strength or would strongly benefit from it. These applications include enhancement of both the high-harmonic generation efficiency^[5] and the cut-off frequency^[6], orientation of molecules^[12,13], electron^[9,10,15,19] and proton^[8] acceleration or other manipulation^[7,17,18], and generation of very special carrier-envelope stable attosecond pulses^[11]. In addition to the above indicated megavolts (MV)/cm range of electric field, some of the previously mentioned applications also require well controllable single- or few-cycle THz pulses. For example,

(i) alignment and orientation of molecules^[12,13] and (ii) efficient particle acceleration and manipulation^[9,10,14] are types of such applications. (i) The degree of both field-free orientation and alignment induced by single-cycle THz pulses with μJ energies in an OCS gas sample was calculated and demonstrated in Refs. [12,13]. However, very recently, the advantage of applying single-cycle THz pulse with MV/cm level field strength was demonstrated^[20]. Numerical calculation predicted maximal orientation degrees for a single-THz pulse with 8 MV/cm field strength. (ii) Using a waveguide structure, which was pumped by $\sim 30 \mu\text{J}$ THz pulse, 200 MV/m acceleration gradient with $\sim 70 \text{ keV}$ energy gain was demonstrated, and the final electron energy of million electron volt (MeV) level was predicted by applying THz pulses with few-MV/cm peak electric field strength^[19]. Another promising alternative accelerator scheme is the THz-driven inverse free-electron laser^[18]. In the first demonstration, 150 keV electron energy modulation was achieved in a magnetic undulator using $\sim 1 \mu\text{J}$ single-cycle THz pulse. Based on the calculations, the energy gain and acceleration gradient scaled linearly with the field of the THz pulse. Thereby, there is room for 2–3 orders of magnitude increase of the energy gain by increasing the THz field. Because of these and other important application possibilities, there is a strong need for developing THz sources that produce pulses with an extremely high field, having a few tens of MV/cm peak electric field strength^[21].

In recent years, disadvantageous properties of the conventional TFPF setup have been identified^[21–26]. These result in the hindrance of simple upscaling of the generated THz energy and field strength by increasing the pumping energy and the pumped area. However, nowadays, a few proposed setups promising mitigation or even elimination of these limitations were numerically investigated^[22,23,26–34]. Although, the papers proposing the new setups usually compare the given new setups with the conventional TFPF setup, a comprehensive comparison of the newly suggested TFPF setups both to each other and to the conventional TFPF setup is missing yet. The present paper aims to present such a comparison.

In Sections 2 and 3, we shortly describe the most critical limiting properties of the conventional TFPF setup and describe the five newly proposed setups for mitigating/eliminating these limitations. In Section 4, we compare the main properties and best application possibilities of these setups.

2. Limitations of the Conventional TFPF Setup

The conventional TFPF THz source is shown schematically in Fig. 1(a). It contains three main optical elements: (1) an optical grating to introduce a pulse front tilt, (2) a lens or optical telescope to image the tilted pulse into the LN NM, and (3) a prism-shaped LN crystal with a wedge angle of γ . Please note that the γ tilt angle inside the LN crystal is set in three steps. First, the grating introduces a tilt angle γ_g . Its tangent will be changed by the imaging system [e.g., the lens in the case of Fig. 1(a)] having M magnification. With the pump beam entering from the air ($n_{\text{air}} \approx 1$) into the LN prism having n_p^{gr} group index, the tangent

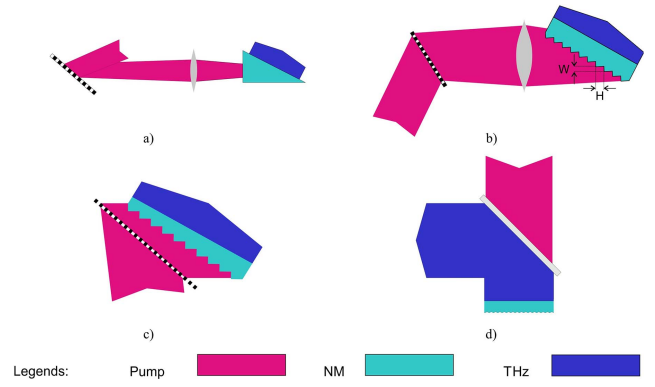


Fig. 1. Schematic depiction of the analyzed setups: (a) conventional TFPF (using optical grating) or TFPF setup with reflective echelon grating, (b) hybrid-contact-grating (with optical grating on NM) and NLES-I and echelon grating on NM, (c) NLES-wol setup, and (d) RNLS setup. See text for details.

of the tilt angle will be decreased by n_p^{gr} times. So, the tangent of γ is given as

$$\tan \gamma = \frac{1}{n_p^{\text{gr}} M} \tan \gamma_g. \quad (2)$$

Since for LN $n_{\text{THz}}^{\text{ph}}$ is more than two times larger than n_p^{gr} , according to Eq. (1), γ has to be larger than 60° . The necessarily large tilt angle and the correspondingly large angular dispersion of the pump beam [see Eq. (3), where n_p^{ph} is the phase index of refraction of the LN at the λ pump wavelength, and $\frac{d\theta}{d\lambda}$ is the angular dispersion of the pump beam^[35]] result in three types of phenomena that cause serious difficulties or create limitations to increasing the peak electric field strength of the generated THz pulses:

$$\tan \gamma = \frac{n_p^{\text{ph}}}{n_p^{\text{gr}}} \lambda \frac{d\theta}{d\lambda}. \quad (3)$$

These limitations are the following:

- (i) Imaging errors in the presence of angular dispersion result in significantly increased pump pulse duration at the edges of a large pump spot^[26,27]. The longer pulse means reduced pump intensity and reduced local pump-to-THz conversion efficiency.
- (ii) The prism shape of the LN crystal results in THz pulses with different temporal shapes across the THz beam cross section because of the different generation lengths. Such a bad quality, strongly asymmetric THz beam cannot be tightly focused, and thus high THz field strength cannot be achieved.
- (iii) Due to the large group-delay dispersion (GDD) associated with the angular dispersion^[35], an ultrashort pump pulse evolves very fast inside the LN crystal. Consequently, the average pulse duration becomes much longer than the Fourier transform-limited (FL) pump pulse duration, resulting in strongly reduced effective

THz generation length and pump-to-THz conversion efficiency^[22].

We notice that the negative effect of the limitation (iii) is less severe for longer FL pump pulses^[22,36–38] since, in this case, because of the smaller spectral bandwidth, the pump pulse evolves more slowly inside the LN.

3. Setups with Reduced/Eliminated Limitations

The following setups for TFPF LN THz sources with reduced or eliminated limitations have been proposed and numerically simulated.

3.1. Hybrid-contact-grating setup

In principle, limitations (i) and (ii) can be entirely eliminated with the application of the contact-grating setup^[27–29,39], which was proposed quite early^[27]. An efficient contact-grating setup was realized using a ZnTe semiconductor as an NM, and as high as 0.3% pump-to THz energy conversion efficiency was demonstrated^[40]. Contact-grating setups were designed and realized for LN too^[28,29]. However, because of technical difficulties induced by the large necessary tilt angle (the need of a good quality contact grating with as high as about 3000 mm^{−1} groove density and the need to use an in-coupling prism^[28]), efficient generation of THz pulses by using an LN contact-grating THz source has failed.

A new version of the contact-grating setup, the so-called hybrid-contact-grating setup, eliminates these difficulties. Here, the γ tilt angle needed for velocity matching is introduced in two steps^[26]. An optical-grating-based imaging system introduces a $\gamma_{\text{pre}} \approx \gamma$ pre-tilt, which without the effect of the contact grating would be reduced according to $\arctan[(\tan \gamma_{\text{pre}})/n_p^{\text{gr}}]$ when the pump pulse enters into the LN. As mentioned above in Eq. (2), such a reduction also happens in the case of the conventional TFPF setup. Because of this, in that case, the grating in the lens system has to introduce a γ_{air} tilt angle according to $\tan \gamma_{\text{air}} = n_p^{\text{gr}} \tan \gamma$. However, in the hybrid-contact-grating setup, the diffraction of the pump beam on the contact grating at the entrance surface of the LN crystal introduces an additional tilt, ensuring the necessary tilt angle γ inside the LN crystal. The substantial advantage of this setup compared with the original contact-grating setup^[27] is the reduced groove density of the contact grating from about 3000 to below 2000 mm^{−1}. This reduction makes the preparation of the contact grating feasible in good quality. The other advantage is that there is no need for an in-coupling prism^[26]. Although the LN still needs to be wedged, the wedge angle ($\leq 30^\circ$) is less than half of that in the conventional TFPF setup. Furthermore, the imaging error becomes also significantly smaller, so larger pump spot size can be used.

3.2. Setup with reflective echelon grating

In order to eliminate limitation (iii), a THz setup that replaces the optical grating with an echelon grating in the conventional

TFPF setup [see Fig. 1(a)] has been proposed and investigated^[30]. Demonstrating the effective elimination of limitation (iii), 0.33% energy conversion efficiency was achieved with pumping by 70-fs-long pulses. It is worth noting that although the pump intensity front inside the LN crystal is segmented (not continuous, it contains beamlets), the tilt angle of the average intensity front is the same as for the conventional TFPF setup. Consequently, the same angular dispersion could be present for long pump pulses^[41]. However, for pump pulses shorter than the delay between the neighboring segments (beamlets) of the pump intensity front, the beamlets cannot interfere with each other, and the divergence of the whole beam is determined by the diffraction of the segment, which is smaller than the product of the angular dispersion [determined by Eq. (3)] and the spectral bandwidth of the pump pulse.

Since this setup contains a prism-shaped LN with the same wedge angle as the conventional TFPF setup, limitation (ii) is similarly effective in hindering using large pump spots and achieving extremely high THz energy.

3.3. Nonlinear echelon slab with imaging

This setup is depicted schematically in Fig. 1(b)^[31]. Similarly to the hybrid-contact-grating setup, this is also a hybrid setup. An optical-grating-based imaging system is used to introduce a pre-tilt angle of γ in the air in front of the LN slab. An echelon structure with W step width and H step depth is manufactured into the originally plane parallel LN slab's front surface. Choosing an

$$\frac{H}{W} = \tan \gamma \quad (4)$$

ratio and tilting the LN slab by an angle of γ , the pump beam arrives perpendicularly to the steps, and the tilt angle of the envelope of the intensity front inside the LN is γ . The THz pulse generated by this pump intensity front will propagate perpendicularly to both the tangential planes of the front and back surfaces of the LN slab, and it will exit from the crystal without refraction. Inside the LN slab, the intensity front is segmented, but, contrary to the case of the reflection echelon grating setup, the intensity fronts in the beamlets are tilted, resulting in less significant “decoherence” (see Section 4.1) for the same W step (beamlet) width. Since introducing γ tilt angle in the air needs smaller angular dispersion than introducing the same γ tilt inside LN, a smaller angular dispersion is present in the pump beam for the nonlinear echelon slab with imaging (NLES-I) setup than for the conventional setup. The smaller angular dispersion results in two disadvantages: both limitations (i) and (iii) become serious. A larger pump spot size can be used, leading to equal pulse elongation in the center and at the edges of the beam, and thus the effective THz generation length becomes much longer.

3.4. Nonlinear echelon slab without imaging

This setup, depicted schematically in Fig. 1(c)^[33], differs from the NLES-I setup in two points. (1) In order to eliminate limitation (i), it does not contain an imaging element. Only a transmission grating is used to introduce the pulse front tilt. (2) Since the transmission grating is used in a symmetric (Littrow) arrangement to maximize its diffraction efficiency, a spatially varying chirp is present in the pump pulse after the diffraction. This effect is compensated by using wedged LN. The wedge angle is typically smaller than 10° . Different pre-tilt angles (typically in the range of 50° – 70°) can be used for different situations. An essential property of the setup is that for about 69° pre-tilt angle and 9° LN wedge angle, the temporal shape of the THz pulses is almost perfectly independent of the transversal position. That is, despite the wedge shape of the LN crystal, spatially homogeneous THz pulses can be generated with a large beam size.

3.5. Reflective nonlinear slab

This setup, depicted schematically in Fig. 1(d)^[34], is the simplest and most compact one. It has only a plane parallel LN slab with a back surface that is structured to form a blazed reflective grating or, for a rougher structure, a reflective echelon. The pump beam comes from the top of the figure. It practically does not generate any THz radiation when it propagates downward inside the LN since the velocity matching condition is not met. However, after it is diffracted or reflected on the structured backside, the velocity matching condition is fulfilled for the two partial beams (not shown in the figure), and THz radiation is generated.

Here, we mention that the type of the diffraction on the back surface depends on the relation between the d period of the structure and the pump pulse duration. If the grating constant is large compared to the product of the pulse duration and the speed of light in LN, the individual parts of the beam cannot interfere with each other. In this case, the structure works as an echelon, and the tilted pulse front will be segmented. For this case, the reflective nonlinear slab (RNLS) works as a reflective nonlinear echelon slab (RNLES). In the opposite case, the structured back surface behaves like a special blazed reflection grating.

4. Comparison of the New Setups

THz generation is examined in detail from two aspects. On the one hand, the generation efficiency of the different setups is investigated at the typical pump wavelengths and pulse duration. On the other hand, the opportunity of the single-cycle THz pulse generation is analyzed. After that, the different setups are evaluated by several aspects.

4.1. High-efficiency generation of THz pulses

In the calculations, Yb-doped yttrium aluminum garnet (Yb:YAG) and Ti:sapphire lasers were assumed as pump lasers, as

these types of ultrashort pulse lasers are available with high energy and high efficiency. For THz generation, the most critical differences between these lasers are the FL pulse duration and the wavelength. The shorter FL pulse duration changes faster during THz generation due to the large bandwidth in the presence of angular dispersion, and thereby the average pump intensity and generation efficiency will be significantly reduced. In the case of the shorter pumping wavelength (800 nm), three-photon absorption in LN becomes effective^[42,43]. The free carriers generated by three-photon absorption of the pump result in significantly increased THz absorption. To avoid this effect, moderate pump intensity should be used, resulting in lower THz generation efficiency.

One-dimensional models were used to describe THz generation for the different setups^[31,33,34]. These models calculate THz generation along the propagation direction of the generated THz pulse through the crystal. The effects of angular dispersion and linear dispersion due to the LN crystal were taken into account when the pump pulse duration was evaluated. The nonlinear optical effects on the pump pulse, such as the cascading effect and self-phase modulation^[25], were neglected. Since absorption by free carriers was also neglected, the results are optimistic in the case of 800 nm pumping wavelength. However, they reflect the relationships between the individual setups well.

In NLES and RNLES setups, the pump beam becomes segmented in the LN crystal due to the rough structured input and reflection surfaces of the LN slab, respectively. According to this fact, two significant effects were taken into account in the models. On the one hand, the “decoherence” effect was taken into consideration. By “decoherence,” the following is meant: the THz wavelets generated at the different transversal points of the beamlets arrive with different phase delays at a distant point in the direction of propagation of the generated THz radiation. These phase differences can result in less constructive interference between the wavelets, causing a drop in the THz generation efficiency. On the other hand, the segmented parts of the beam can be considered in the model as independent beamlets^[31,44]. These beamlets are diffracted during the propagation. The diffraction causes a decrease in the intensity of the beamlets, which also influences the generation efficiency negatively.

The dependencies of the efficiencies on the crystal length are presented in Fig. 2 in the case of the two different pump pulse sources for two different temperatures. The velocity matching frequency was supposed to be 0.5 THz in all cases. In order to avoid the damage of the LN crystal and the unwanted nonlinear effects, the intensity was kept at 70 GW/cm^2 and 140 GW/cm^2 in the case of 200 fs and 50 fs pump pulse duration, respectively, similarly to Ref. [33].

According to the calculations, the conventional setup could achieve one of the highest efficiencies in the case of 200 fs FL pump pulses and room temperature operation [see Fig. 2(a)]. However, in this case, the usable beam size is very limited (approximately 1 mm) because of both the decreasing generation efficiency and transversal inhomogeneity of the THz pulse

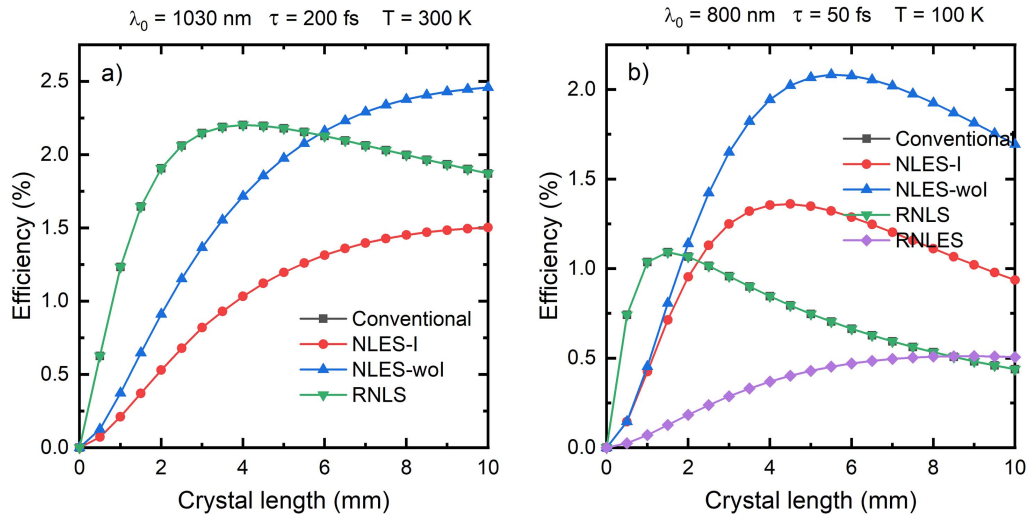


Fig. 2. Dependence of the efficiency on the crystal length using conventional, NLES-I, NLES-wol, and RNLS setups in case of two different pump pulse sources. In the case of an ultrashort pulse source, the RNLES setup was also investigated. The phase matching frequency was 0.5 THz.

shape with increasing pump beam size^[33,45]. As it was mentioned above, the NLES-I setup could be used with a plane parallel LN slab to achieve perfect homogeneity. In this case, 1.5% THz generation efficiency could be approached for large crystal thickness. The beam waist radius of the pump can be 16 mm without significant imaging errors^[31]. Assuming a pump pulse with a super-Gaussian spatial profile and 70 GW/cm² peak intensity, the corresponding pump pulse energy is 90 mJ. So, using this setup, the generated THz energy could be higher than 1 mJ. Using the nonlinear echelon slab without imaging (NLES-wol) setup, a near-perfectly uniform THz beam could also be achieved if the wedge angle is close to 9°^[33]. In this case, only the wedged shape of the crystal limits the beam size at such a large value as 50 mm. With the predicted generation efficiency of more than 2%, this allows generating THz pulses with 15 mJ energy by 750 mJ pump pulse energy. The achievable efficiency by RNLS is similar to the one of the conventional setup. However, in the case of RNLS, there is no limitation for the pumping beam size, and the generated THz energy will be limited only by the pump pulse energy.

In the case of the conventional and RNLS setups, for significantly shorter than 100 fs pump pulse duration, the optimal crystal length is shorter than 2 mm [see Fig. 2(b)]. This is the result of limitation (iii), as is explained in Section 2. The negative effect of the shorter crystal length on the THz generation efficiency can be partly compensated by using cryogenic operation temperature. Since the angular dispersion is two times smaller in the NLES setups than in the conventional and RNLS setups, the reduction of the effective THz generation length with decreasing pump pulse duration is less significant. According to Fig. 2(b), the optimal crystal thickness is 4–5 mm, and the THz generation efficiency is 1.3 and 2.0 times larger than for the conventional and RNLS setups. The advantage of RNLES (in the absence of angular dispersion, only the smaller effect of the material dispersion of the LN crystal influences the

variation of the pump pulse duration inside the crystal) becomes effective in the case of ultrashort (less than 50 fs FL pulse duration) pump pulses.

4.2. Single-cycle THz pulse generation

For many applications, a strict single-cycle temporal shape of the THz pulses has outstanding importance. Therefore, the condition of single-cycle THz pulse generation was investigated for the different setups. Figures 3(a)–3(c) show the amplitude ratio of the side peak [see Fig. 4(a)] of the THz pulse to its mean peak as a function of the pump pulse duration and the crystal thickness. The corresponding THz generation efficiencies are shown in Figs. 3(d)–3(f). The shapes of the generated THz pulses and their spectra are shown in Fig. 4 for $E_{\text{side}}/E_{\text{max}} = 10\%$.

According to Figs. 3(a)–3(c), the longer the pump pulse lengths are, the more single-pulse character the generated THz pulse has. The dispersion can explain this behavior in the THz spectral range. Really, it is expected that in the normal dispersion range the GDD results in such chirping of a traveling ultrashort pulse that the lower frequency appears on the leading part and the higher frequency on the trailing part, in agreement with Fig. 4. Using longer pump pulses, the generated THz frequencies are lower, and the effect of GDD is less significant. Of course, in the case of THz pulse generation in the LN crystal, other effects are also significant, and the dependence of the single-cycle character on the crystal length becomes more complex. For example, according to Fig. 3(a), in the case of NLES, the single-cycle character is almost independent of the crystal length.

So, for shorter than 500-fs-long pump pulses, the NLES setup is recommended for the generation of high-energy THz pulses with excellent beam quality. In the case of longer pump pulse durations, each presented setup is applicable for generating single-cycle THz pulses, but the simplest and most scalable is the RNLS^[34]. It is worth mentioning that using intensity-modulated

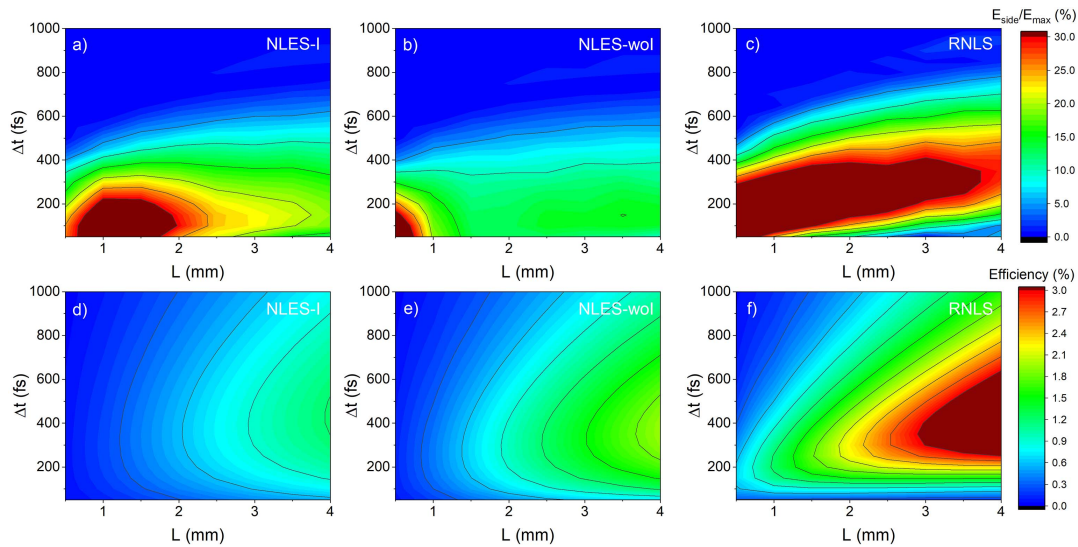


Fig. 3. (a)–(c) Ratio of the side peak to the main peak of the THz pulse and (d)–(f) the efficiency of the THz generation as a function of the pump pulse duration and the crystal thickness, for (a), (d) NLES-I, (b), (e) NLES-wol, and (c), (f) RNLS cases.

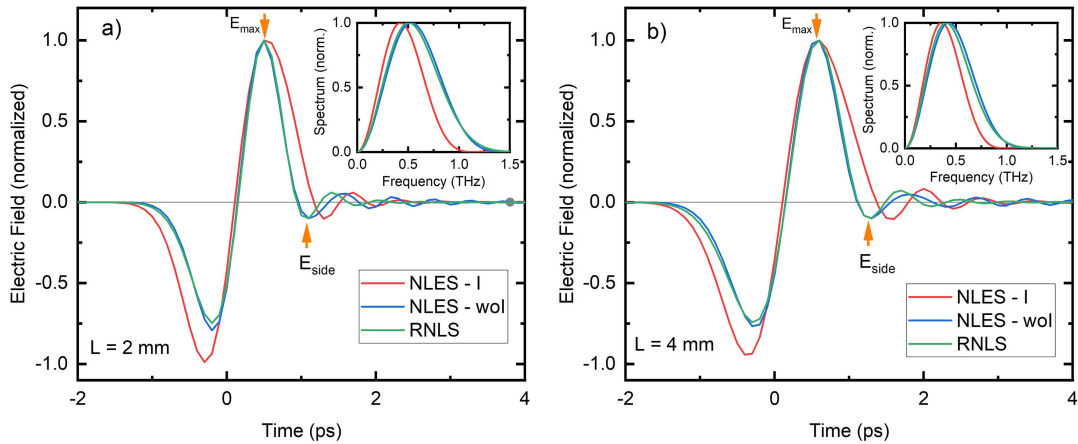


Fig. 4. Shapes and spectra (insets) of the generated THz pulses by NLES-I (red), NLES-wol (blue), and RNLS (green) setups for crystal lengths of (a) 2 mm and (b) 4 mm. The pump pulse duration was appropriately chosen in order to satisfy the $E_{\text{side}}/E_{\text{max}} = 10\%$ ratio. The corresponding pump pulse durations were (a)/ (b) 465 fs/475 fs, 340 fs/390 fs, and 605 fs/700 fs in the cases of NLES-I, NLES-wol, and RNLS, respectively.

pump pulses, all setups are suitable for generating multicycle THz pulses, too. Three important techniques were suggested to generate these kinds of pump pulses: chirp and delay technique^[46–48], dual chirped optical parametric amplification technique^[49], and technique based on the Vernier effect^[50].

4.3. Recommendation

Based on the discussion above and on our experience, we compared the most important properties of the different reviewed setups in Table 1. “Efficiency” means the pumped to THz conversion efficiency. “Scalability” means the energy scalability, which primarily depends on the useable pump beam size. “Beam quality” means the electric field homogeneity of the THz beam along the transversal dimension. “Shape stability” means how independent the waveform of the generated THz

pulse is from the pump pulse length or the crystal length. “Feasibility” shows how easy (or difficult) it is to implement a given setup at the current state of the art.

It is important to note that every setup can work in echelon and optical-grating modes. In the case of echelon mode, the pulse front is discretely tilted, and it is segmented; in the case of conventional-grating mode, the pulse front tilt is continuous. The reflective echelon setups are the same as the conventional setup in the echelon mode. NLES-I is a special hybrid-contact-grating setup in the echelon mode. The mode depends on the size of the grating groove relative to the spatial length of the pulse. If the grooves are not near enough to each other to interfere with the transmitted/reflected parts of the beam, the grating will work as an echelon grating, and the pulse front will be segmented. In the above discussion, including Table 1, it

Table 1. Comparison of the Different THz Generation Setups^a.

	Conventional	Hybrid Contact Grating	Reflection Echelon	NLES-I	NLES-woI	RNLS
Efficiency	+++	++	+++	+	++	+++
Scalability	+	++	+	++	+++	∞
Beam quality	+	++	+	+++	+++	∞
Shape stability	+	++	++	+++	++	+
Feasibility	+++	+	++	+	+	++

^aMore “+” signs mean better, and “∞” means theoretically perfect.

was assumed that the conventional, the hybrid contact grating, and the RNLS setups work in the optical-grating mode, while, the reflection echelon and both NLES setups work in the echelon mode. More sophisticated code^[51] was used to investigate a few of the setups presented here. That model predicts significantly smaller optimal crystal length and lower energy conversion efficiency than ours. However, it supports our main claim that the significant reduction (or even annulling) of the wedge angle of the crystal by the NLES technique results in higher conversion efficiencies and a much better pulse shape that is produced by the conventional setup. It is worth noting that if a smaller than Littrow incidence angle of the pump pulse is used on the grating in the NLES-woI setup, the wedge angle of the crystal could be further reduced^[52]. Furthermore, according to our preliminary experiment^[53], it is possible to use a volume holographic grating (VHG) in the NLES-woI setup at a normal incidence angle without decreasing the diffraction efficiency. In this case, similarly to the NLES-I setup, a plane-parallel slab of LN can be used as NM, and our results obtained for the NLES-I setup become applicable.

5. Conclusion

The fundamental and practical limitations of recently proposed high-energy LN sources were analyzed. We have shown that the NLES-I, NLES-woI, and RNLS pumping schemes can significantly reduce the limitations of the conventional TFPF LN THz source. Performances of the different setups were compared, showing that a very significant enhancement of the available THz pulse energy and excellent beam quality can be expected by using the new setups compared to the conventional one. The only limiting factors are the available pump energy and crystal size in the case of RNLS. The RNLS setup will pave the way to new applications requiring multi-mJ THz pulses. Such critical applications are particle acceleration and manipulation, generation of attosecond pulses by high harmonic generation and other methods, orientation, and alignment of molecules, which all will gain from the availability of THz sources producing focused field strength in the few 10 MV/cm regime.

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