## ARTICLE

### Open Access

# Bound vortex light in an emulated topological defect in photonic lattices

Chong Sheng<sup>1</sup>, Yao Wang<sup>2</sup>, Yijun Chang<sup>2</sup>, Huiming Wang<sup>2</sup>, Yongheng Lu<sup>2</sup>, Yingyue Yang<sup>2</sup>, Shining Zhu<sup>1</sup>, Xianmin Jin<sup>2,3M</sup> and Hui Liu<sup>1</sup>

#### Abstract

Topology have prevailed in a variety of branches of physics. And topological defects in cosmology are speculated akin to dislocation or disclination in solids or liquid crystals. With the development of classical and quantum simulation, such speculative topological defects are well-emulated in a variety of condensed matter systems. Especially, the underlying theoretical foundations can be extensively applied to realize novel optical applications. Here, with the aid of transformation optics, we experimentally demonstrated bound vortex light on optical chips by simulating gauge fields of topological linear defects in cosmology through position-dependent coupling coefficients in a deformed photonic graphene. Furthermore, these types of photonic lattices inspired by topological linear defects can simultaneously generate and transport optical vortices, and even can control the orbital angular momentum of photons on integrated optical chips.

#### Introduction

Photonic lattices<sup>1</sup> made of single-mode coupled waveguides have become a hugely popular tool for simulating a plethora of physical phenomena, ranging from reservoir engineering<sup>2</sup>, demonstration of flat-band states and dispersion-less light propagation<sup>3–6</sup>, topological bandgaps and edge modes<sup>7–9</sup>, to topological pumping<sup>10,11</sup> and Aharonov-Bohm cages<sup>12–14</sup>, etc. Intriguingly, photonic graphene, one of novel types of photonic lattices, have successfully emulated various topological phenomena in condensed matter physics, for example, photonic Floquet topological insulators using spiral waveguides<sup>15</sup>, Landau levels using strain lattices<sup>16</sup>, the unconventional edge states<sup>17,18</sup>, the pseudospin-mediated vortex generation<sup>19</sup>.

Full list of author information is available at the end of the article These authors contributed equally: C. Sheng, Y. Wang.

Additionally, photonic lattices have also allowed for the simulation of quantum physics in general relativity<sup>20-24</sup>, such as fermion pair production<sup>22-24</sup>, hyperbolic space<sup>25,26</sup> with constant negative curvature connecting to anti-de Sitter/conformal field theory correspondence.

On the other hand, a stochastic gravitational wave background<sup>27-29</sup>, which was possibly emitted by a cosmic-string network<sup>27,28</sup> that is a topological linear defect generated in the early Universe, has attracted widespread attention in cosmology. Aside from gravitational waves, theorists have predicted some other interesting nontrivial phenomena about these cosmic topological defects, such as the Aharonov-Bohm interaction of cosmic strings $^{30-32}$  and the spin hall effect influenced by the nontrivial deformation of the space time of cosmic strings<sup>33</sup>. Although these predictions cannot be directly found in astronomy up to now, the theoretical foundations behind these phenomena of general relativity have been extensively applied to condensed matter systems and other various systems. One of the salient examples is the Hawking-Unruh effect near the event horizons, which has been well-emulated using a variety of quantum architectures<sup>34–38</sup>.

Correspondence: Xianmin Jin (xianmin.jin@sjtu.edu.cn) or Hui Liu (liuhui@niu.edu.cn)

<sup>&</sup>lt;sup>1</sup>National Laboratory of Solid State Microstructures and School of Physics, Collaborative Innovation Center of Advanced Microstructures, Nanjing University, Nanjing, Jiangsu 210093, China

<sup>&</sup>lt;sup>2</sup>Center for Integrated Quantum Information Technologies (IQIT), School of Physics and Astronomy and State Key Laboratory of Advanced Optical Communication Systems and Networks, Shanghai Jiao Tong University, Shanghai 200240, China

<sup>©</sup> The Author(s) 2022

Open Access This article is licensed under a Creative Commons Attribution 4.0 International License, which permits use, sharing, adaptation, distribution and reproduction in any medium or format, as long as you give appropriate credit to the original author(s) and the source, provide a link to the Creative Commons license, and indicate if changes were made. The images or other third party material in this article are included in the article's Creative Commons license, unless indicated otherwise in a credit line to the material. If material is not included in the article's Creative Commons license and your intended use is not permitted by statutory regulation or exceeds the permitted use, you will need to obtain permission directly from the copyright holder. To view a copy of this license, visit http://creativecommons.org/licenses/by/4.0/.

At the same time, transformation optics<sup>39,40</sup> which was inspired by general relativity has provided a new method to design artificial materials with novel optical functions. One fascinating example is invisibility cloaks<sup>41-43</sup>, in which light is regarded as linear parallel geodesic rays in deformed spaces. Additionally, other examples include the light trapping<sup>44-48</sup> by emulating black holes, the illusion electromagnetic devices<sup>49</sup>, the definite electromagnetic scattering<sup>50</sup> in the emulated nontrivial space and the wavefront shaping 51-53 on curved space, etc. However, all these novel transformation optics devices were constructed by emulating space without a gauge field. Indeed, some general relativity phenomena $^{30-33}$  involve both a gravitational field and a gauge field. And what novel optical application will be brought by the design, which simulates a gravitational field and a gauge field at the same time, is rarely experimentally reported.

Recently, there has been an increasing interest in optical vortices that have wide-ranging applications in micromanipulation<sup>54</sup>, free-space communications<sup>55</sup>, and quantum information technology<sup>56</sup>. The generation of optical vortices has been investigated for various optical eleincluding computer-generated holograms<sup>57</sup>, ments, inhomogeneous anisotropic media<sup>58</sup>, angular gratings inside microrings<sup>59</sup>, and metasurfaces<sup>60</sup>. However, in most of the reported works, the generated vortex states mainly radiate in free space, whereas there are few works regarding the simultaneous generation and transportation of vortex states on photonic chips. In contrast, the development of integrated optical chips requires a simple scheme to perform the simultaneous generation and transmission of optical vortices on chips. Although the doughnut-shaped waveguide<sup>61,62</sup> on a photonic chip has been experimentally exploited to generate and transmit optical vortices, this type of generation has the aid of an external auxiliary waveguide. The simultaneous generation and transmission of optical vortices in the same process has rarely been reported.

In this work, we exploited a deformed photonic graphene, a novel type of photonic lattices, to map massless Dirac fermions in the presence of the gauge field of a cosmic string. We experimentally realized bound vortex light by simulating the gauge field of such a cosmic string. Our approach is to deform the photonic graphene lattice by deliberately tuning the coupling coefficient as a function of the position according to the effective Hamiltonian after considering the massless Dirac equation in the presence of such a topological linear defect. The required anisotropic velocity of Dirac fermion in the polar coordinate are obtained by the designed anisotropic and nonuniform coupling coefficient. Meanwhile, such designed coupling coefficients also shift the Dirac cone in the momentum space to yield the required gauge field. Very recently, the topological lattice defects<sup>63</sup> in Weyl crystals were demonstrated to bind acoustic vortex states through a judicious "cut-and-glue" procedure. Compared to the generation of topological defects through the deficit of the physical structure, we leverage the position-dependent coupling coefficient in a photonic graphene to emulate the cosmic string. Remarkably, such photonic lattices can simultaneously generate and transport optical vortex modes nearly without diffusion, and even have an ability to manipulate the angular momentum of photons on a photonic chip.

#### Results

# The mapping of the Dirac equation of cosmic stings into photonic lattices

To study the vortex bound Dirac fermion mode in the presence of cosmic strings, we began with the massless Dirac equation with a gauge field in the curved space as follows<sup>64,65</sup>:

$$\gamma^{u}(\partial_{u} + \Omega_{u} + iA_{u})\psi = 0 \tag{1}$$

where  $\gamma^{\mu}$  is the Dirac matrix in a curved background,  $\Omega_{\mu}$  is the spinor connection, and  $A_{\mu}$  is the electromagnetic gauge potential. In the following, we will focus our calculations on the cosmic-string space time at a certain plane (see Fig. 1a), and the line element is given by

$$ds^2 = -dt^2 + dr^2 + \alpha^2 r^2 d\theta^2 \tag{2}$$

where  $\alpha = 1 - 4G\mu/c^2$  is the density parameter that corresponds to the deficit angle, G is the gravitational constant,  $\mu$  and c are respectively the linear mass density of the cosmic string and the speed of light. After considering the spacetime metric of cosmic strings, we obtain spinor connection  $\Omega_{\theta} = \frac{i}{2}(1-\alpha)\sigma_z$ . Furthermore, considering that the cosmic string has electromagnetic gauge potential with  $A_x = \eta \sin 2\theta$ ,  $A_y = \eta \cos 2\theta$  ( $\eta =$  $-(1-\alpha)/(1+\alpha)$  is the amplitude of the gauge field), we obtained the Dirac fermion with anisotropic velocities for the radial and angular direction as  $v_r/v_{\theta} = \alpha$  and the gauge field as  $A_r = \eta \sin 3\theta$ ,  $A_\theta = \alpha r \eta \cos 3\theta$  (see details in the Supplementary Section I). Hence, both the anisotropy of the velocity and the gauge field for the massless Dirac fermion were decided by the mass density parameter  $\alpha$  of the cosmic string. For the case of the flat space ( $\alpha = 1$ ), the massless Dirac fermion had isotropic velocity and was not subjected to a gauge field. For the case of cosmic strings with a deficit angle ( $\alpha < 1$ ), we could obtain the massless Dirac fermion with anisotropic velocity and a nonzero gauge field. Moreover, both the anisotropy of the fermion velocity and the amplitude of the gauge field increased with the increases of the deficit angle of the cosmic string.



To construct the quantum field of Dirac fermions in the presence of cosmic strings, we chose a deformed photonic graphene lattice (Fig. 1b) as a real system that was as close as possible to the required quantum field<sup>20</sup>. We considered that the hopping between the nearest sites was space dependent, and in general, it was characterized by three hopping parameters  $t_1$ ,  $t_2$ , and  $t_3$ . Within this nearest-neighbor tight-binding model, one could demonstrate that the effective Dirac Hamiltonian could be obtained by expanding the Hamiltonian around a corner, e.g.,  $\vec{K}_0 = \left(0, \frac{4\pi}{3\sqrt{3}a}\right)$  for the isotropic case  $t_{1,2,3} = t_0$ . However, for the anisotropic case<sup>66</sup>  $t_1 = t_0(1 + \eta \cos 2\theta), \quad t_2 = t_0(1 - \eta \cos(2\theta - \frac{\pi}{3})), \quad t_3 =$  $t_0(1 - \eta \cos(2\theta + \frac{\pi}{3}))$  as shown in Fig. 1d, and one could determine that the Dirac point  $\vec{K}_D$  was given by  $\vec{K}_D =$  $\vec{K}_0 + \vec{A}$  (see Fig. 1c), where  $\vec{A}$  is the gauge field given by  $A_x = \eta \sin 2\theta, A_y = \eta \cos 2\theta$ , circling around the origin of the cosmic strings (For the case that  $\vec{K}_0$  with valley index -1 see details in the Supplementary Section II). Moreover, one could obtain an effective Dirac Hamiltonian (see details in the Supplementary Section II):

$$E_F = \hbar \nu'_F i \sigma_z \vec{\sigma} \cdot U^{-1}(\theta) \begin{pmatrix} \alpha & 0 \\ 0 & 1 \end{pmatrix} U(\theta) \cdot \vec{q}$$
(3)

where  $v'_F$  is the reduced Fermi velocity for the massless Dirac fermion,  $\vec{\sigma} = (\sigma_x, \sigma_y)$  represents the non-diagonal Pauli matrices,  $\sigma_z$  is the diagonal Pauli matrix,  $\vec{q}$  is the momentum vector, and  $U(\theta) = \begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix}$  is the rotation operator. Based on the effective Dirac Hamiltonian and the shift of the Dirac cone in the momentum space, the Dirac fermion conducted by the deformed photonic graphene had the anisotropic velocity of  $v_r/v_\theta = \alpha$ a and it was subjected to the gauge field with  $A_r = \eta \sin 3\theta$ ,  $A_\theta = \alpha r \eta \cos 3\theta$ , which satisfied the condition required by the quantum field of massless Dirac fermions in the presence of cosmic strings.



sites. **h** is the bound index as the excitation of a single waveguide on different ring layers. The theoretical calculation was carried out in the graphene lattice whose size was 1302 waveguide sites. Whereas considering the limitation of experimental fabrication, the experimental results were determined using a graphene lattice with 150 waveguide sites

# The generation and transmission of vortex states in the emulated cosmic strings

To construct the coupling coefficients as required by emulating cosmic strings, we exploited the femtosecond laser direct writing technique to fabricate single-mode waveguides in borosilicate glass. Since the coupling strength drops quite steeply with the distance, only the nearest-neighbor coupling is considered. Owing to the fabrication advantages of femtosecond laser direct writing that can freely prototype waveguides as sites of lattices and precisely control coupling in three dimensions, the deformed photonic graphene (as shown in the inset of Fig. 3e) had space dependent nearest-neighbor coupling coefficients and it could emulate the cosmic string with a gauge field. Because such an evanescently coupled waveguide array rendered the evolution of photons for the Schrödinger-like equation and allowed us to directly observe the quantum dynamics, we could directly study the quantum evolution for the emulated cosmic string with a gauge field.

In experiments, we successfully observed a vortex bound fermion mode in the deformed photonic graphene. Figure 2a, b clearly exhibit the confined photons evolving around the cosmic string and propagating with different distances after the photons were injected into a single waveguide site (the details of such bound states from the tight-binding model in Supplementary Section III, IV). Although a small amount of the energy radiated out, the energy that circled around the cosmic string was dominant. As expected, the confinement of the injected photons into different sublattice sites of the innermost layer exhibited the same behavior (see Fig. S3 in the Supplementary). In comparison, there were only radiating modes in flat space (analogous to unperturbed photonic graphene) and the energy could not be trapped any more, as shown in Fig. 2c and d. To quantify the diffusion size of the bound vortices for the different gauge fields of the emulated cosmic string, we show the proportion of the photon distribution among the sites outside the innermost layer in Fig. 2e. The photons were strongly localized around the cosmic string with the density parameter  $\alpha_1 = 1/2$ , slightly localized for the case with the density parameter  $\alpha_2 = 2/3$ , and widely diffused in flat space ( $\alpha_3 = 1$ ). These phenomena distinctly clarified the fact that the emulated cosmic string with a larger deficit angle had a larger amplitude of the gauge field, leading to a higher capability to confine photons into a vortex. Although the losses and imperfections induced by fabrication and materials were unavoidable in experiments, the experimental results were agreement with the theoretical calculation.



Furthermore, the magnetic field in the presence of the cosmic string had the form of  $B_z \propto 1/r$ , and the magnetic field strength decayed with the distance away from the cosmic string (see details in the Supplementary Section I). Hence, the confinement ability of the photons decreased with the distance away from the cosmic string, as shown in Fig. 2f. In the experiment, we injected the photons into a single site in the first layer, second layer, and third layer along the vertical direction, and as theoretically expected, the photons gradually diffused (see Fig. 2g). We defined the bound index as the proportion of the photon distribution into the innermost layer among all sites (the range between white dashed lines in Fig. 2g). The result of the bound index shown in Fig. 2h accurately reflected the decay of the magnetic field strength with the distance away from the cosmic string.

#### Bound vortices around the emulated cosmic string

To further the theoretical understanding of the bound vortices around the cosmic string, one could solve the Hamilton equation. Although there was not a general analytical solution for the equation, one could obtain an approximate solution as  $\psi_e = \left(r^{-\frac{w}{a}}e^{-im\theta}, r^{-\frac{u}{a}}e^{in\theta}\right)^T$  with the angular momentum *m* and *n* near the origin of the cosmic strings (see details in the Supplementary Section I). The case of  $m \le 0$  and  $n \le 0$  corresponded to a radiating mode with the increasing intensity  $I = |\psi_e \psi_e^*|$  for the large distance. In contrast, the case as m > 0 and n > 0 corresponded to a bound state with the decreasing intensity  $I = |\psi_e \psi_e^*|$  with the large distance, and the energy distribution was confined around the origin. Therefore, this

nontrivial property could confine vortex modes with positive vortex charges. Additionally, this nontrivial property indicated that bound vortices circled around in a clockwise direction, but the reverse was not allowable (see the Supplementary videos). With the excitation of one single waveguide in the innermost ring layer around the cosmic string, one could assume that the excitation state was the superposition of the Dirac fermion with many different vortex charges. Although some energy radiated out, a large portion of energy was confined and twisted around the string with a clockwise direction.

To clearly exhibit bound vortices for the gauge field of the cosmic string in experiments, we also fabricated a 1×3 coupler before the lattice and connected it to three sites with the same sublattice in the innermost layer, as shown in Fig. 3e. By exciting the input waveguide of the 1×3 coupler, we could the obtain initial state  $|\varphi_{in}\rangle = \sum_{n} e^{i\theta_i} |i\rangle$ as the vortex fermion mode, where *i* ranged from 1 to 3 as the site label, and  $\theta_i$  was the phase magnitude for the *i*th site (see details in section IV in the Supplementary). By modulating the hopping and the on-site energy in the fabrication, we obtained the initial state  $|\varphi_{in}\rangle$  with  $\theta_1 \neq \theta_2 \neq \theta_3$  and injected it into the lattice. As shown in Fig. 3d, the optical vortex mode was well-bound for the gauge field of the cosmic string but not in the flat space. As illustrated in Fig. 3f, we compared the diffusion size for the evolution distance for different density parameters, which distinctly showed that the emulated cosmic string with a smaller density parameter, corresponding to a larger magnitude of the gauge field, had a stronger confinement capability.



Furthermore, this type of deformed photonic graphene inspired by cosmic strings has the capability of distinguishing photons with or without orbital angular momentum. Unlike photons with orbital angular momentums, when the electromagnetic waves without orbital angular momentum  $(l_{OAM} = 0)$  were injected into this type of deformed photonic graphene, the radiation modes were excited and diffused to all sites in the lattice, as shown in Fig. 4a, which was the natural result of the wave dynamics near the Dirac point (see Fig. S1 in Supplementary). We directly injected the vortex beams with different charges, such as,  $l_{OAM}=0$ ,  $l_{OAM}=1$  and  $l_{OAM}=$ 2, into the deformed photonic graphene lattices from the innermost ring layer in the experiments. Then we experimentally measured the evolution results for the same propagation (50 mm), as shown in Fig. 4e-g. Figure 4h shows the quantified diffusion size for different cases for different orbital angular momentums and the gauge fields of cosmic strings. These results clarified the fact that the light with orbital angular momentum in the emulated large gauge field of cosmic strings exhibited a well-defined local confinement, whereas the light spread for the case without orbital angular momentum. Hence, the deformed photonic graphene had the capability of distinguishing photons with or without orbital angular momentum. While the current deformed photonic graphene cannot distinguish different charges of angular momentums just as shown in Fig. 4c and d that indicates the evolution patterns are almost same with inputting different angular momentums. In the following work, we will change the design of the deformed photonic graphene to have the capability for distinguishing photons not only whether with angular momentums but also with the charge of angular momentums.

#### Discussion

In summary, we exploited a deformed photonic graphene lattice to simulate a gauge field of topological cosmic string. The deformed photonic lattice inspired by topological cosmic strings could generate and transport optical bound vortices at the same time, and even manipulate the angular momentum of photons on a chip. This novel feature may have potential applications on integrated photonic chip. In this work, we just emulated the gauge field of cosmic strings through effective Dirac Hamiltonian in a deformed photonic graphene. Whereas other issues of cosmic strings, such as their creation and dynamics during early-time evolution of the universe, may be mapped into another type of photonic lattices. Additionally, the design of bound states can also be utilized to enhance nonlinearity of optical fibers, which may make them as quantum light source in photonic computing. Furthermore, the developed experimental platform of photonic lattices also has a potential in neuromorphic quantum computer<sup>67,68</sup> inspired by the mechanism of memristor.

#### Materials and methods

We fabricate the designed photonic lattice using the femtosecond laser direct writing technology. We fabricate the samples in borosilicate glass substrate (refractive index  $n_0 = 1.514$  for the writing laser) using the femtosecond laser system operating at a wavelength of 513 nm, a repetition rate of 1 MHz and a pulse duration of 290 fs. The light is reshaped with a cylindrical lens and then is focused inside the sample with a 50× microscope objective (NA = 0.55). The substrates are continuously moved using a high-precision three-axis translation stage with a constant velocity of 10 mm/s, and the lattices are created by the laser-induced refractive index increase. For each a waveguide in the photonic lattice, it supports a single-mode waveguide for the propagation of wavelength at 810 nm. And the characterized relationship of the coupling coefficients and the separation between adjacent waveguides satisfies the formula as  $t = 3.30 e^{-0.19d}$ . And d is the distance between adjacent waveguide sites. According to such a relation, we arrange the distance of waveguide site in a deformed photonic graphene to realize the designed anisotropic and nonuniform coupling coefficients required by emulating such a topological linear defect.

#### Acknowledgements

This work was financially supported by the National Key R&D Program of China (Grant Nos. 2017YFA0303700, 2017YFA0303702, 2017YFA0205700), the National Natural Science Foundation of China (Grant Nos. 12174187, 11690033, 92163216, 92150302, 61425018, 11621091), and the Fundamental Research Fund for the Central Universities, China (Grant No. 14380139, 14380191).

#### Author details

<sup>1</sup>National Laboratory of Solid State Microstructures and School of Physics, Collaborative Innovation Center of Advanced Microstructures, Nanjing University, Nanjing, Jiangsu 210093, China. <sup>2</sup>Center for Integrated Quantum Information Technologies (IQIT), School of Physics and Astronomy and State Key Laboratory of Advanced Optical Communication Systems and Networks, Shanghai Jiao Tong University, Shanghai 200240, China. <sup>3</sup>CAS Center for Excellence and Synergetic Innovation Center in Quantum Information and Quantum Physics, University of Science and Technology of China, Hefei 230026, China

#### Author contributions

S.N.Z., H.L., C.S., and X.M.J. conceived and supervised the project. Y.W. and Y.J.C. fabricated the samples. Y.W., Y.J.C., Y.H.L., and Y.Y.Y. performed the measurements. C.S. conducted the theoretical analysis. C.S. and Y.W. analyzed the data and wrote the paper with input from all authors.

## Competing interests

The authors declare no competing interests.

Supplementary information The online version contains supplementary material available at https://doi.org/10.1038/s41377-022-00931-4.

Received: 10 March 2022 Revised: 10 July 2022 Accepted: 11 July 2022 Published online: 01 August 2022

#### References

- Szameit, A. & Nolte, S. Discrete optics in femtosecond-laser-written photonic structures. J. Phys. B: At. Mol. Optical Phys. 43, 163001 (2010).
- Klauck, F. et al. Observation of PT-symmetric quantum interference. Nat. Photonics 13, 883–887 (2019).
- Mukherjee, S. et al. Observation of a localized flat-band state in a photonic Lieb lattice. *Phys. Rev. Lett.* **114**, 245504 (2015).
- Vicencio, R. A. et al. Observation of localized states in Lieb photonic lattices. *Phys. Rev. Lett.* **114**, 245503 (2015).
- Biesenthal, T. et al. Experimental realization of PT-symmetric flat bands. Phys. Rev. Lett. 123, 183601 (2019).
- Wang, P. et al. Localization and delocalization of light in photonic moiré lattices. Nature 577, 42–46 (2020).
- Maczewsky, L. J. et al. Observation of photonic anomalous Floquet topological insulators. *Nat. Commun.* 8, 13756 (2017).
- Mukherjee, S. et al. Experimental observation of anomalous topological edge modes in a slowly driven photonic lattice. *Nat. Commun.* 8, 13918 (2017).
- Pyrialakos, G. G. et al. Symmetry-controlled edge states in the type-II phase of Dirac photonic lattices. *Nat. Commun.* 11, 2074 (2020).
- Kraus, Y. E. et al. Topological states and adiabatic pumping in quasicrystals. *Phys. Rev. Lett.* **109**, 106402 (2012).
- Zilberberg, O. et al. Photonic topological boundary pumping as a probe of 4D quantum Hall physics. *Nature* 553, 59–62 (2018).
- Longhi, S. Aharonov-Bohm photonic cages in waveguide and coupled resonator lattices by synthetic magnetic fields. *Opt. Lett.* **39**, 5892–5895 (2014).
- Mukherjee, S. et al. Experimental observation of aharonov-bohm cages in photonic lattices. *Phys. Rev. Lett.* **121**, 075502 (2018).
- Kremer, M. et al. A square-root topological insulator with non-quantized indices realized with photonic Aharonov-Bohm cages. *Nat. Commun.* 11, 907 (2020).
- Rechtsman, M. C. et al. Photonic Floquet topological insulators. Nature 496, 196–200 (2013).
- Rechtsman, M. C. et al. Strain-induced pseudomagnetic field and photonic Landau levels in dielectric structures. *Nat. Photonics* 7, 153–158 (2013).
- Plotnik, Y. et al. Observation of unconventional edge states in 'photonic graphene'. Nat. Mater. 13, 57–62 (2014).
- Rechtsman, M. C. et al. Topological creation and destruction of edge states in photonic graphene. *Phys. Rev. Lett.* **111**, 103901 (2013).
- Song, D. H. et al. Unveiling pseudospin and angular momentum in photonic graphene. Nat. Commun. 6, 6272 (2015).
- Iorio, A. & Lambiase, G. Quantum field theory in curved graphene spacetimes, Lobachevsky geometry, Weyl symmetry, Hawking effect, and all that. *Phys. Rev.* D. 90, 025006 (2014).
- Lustig, E. et al. Curved-space topological phases in photonic lattices. *Phys. Rev.* A 96, 041804 (2017).
- Dreisow, F. et al. Vacuum instability and pair production in an optical setting. *Phys. Rev. Lett.* **109**, 110401 (2012).
- Koke, C., Noh, C. & Angelakis, D. G. Dirac equation in 2-dimensional curved spacetime, particle creation, and coupled waveguide arrays. *Ann. Phys.* 374, 162–178 (2016).
- 24. Wang, Y. et al. Quantum simulation of particle pair creation near the event horizon. *Natl Sci. Rev.* **7**, 1476–1484 (2020).
- Boettcher, I. et al. Quantum simulation of hyperbolic space with circuit quantum electrodynamics: from graphs to geometry. *Phys. Rev. A* **102**, 032208 (2020).
- Kollár, A. J., Fitzpatrick, M. & Houck, A. A. Hyperbolic lattices in circuit quantum electrodynamics. *Nature* 571, 45–50 (2019).

- Ellis, J. & Lewicki, M. Cosmic string interpretation of NANOGrav pulsar timing data. *Phys. Rev. Lett.* **126**, 041304 (2021).
- Blasi, S., Brdar, V. & Schmitz, K. Has NANOGrav found first evidence for cosmic strings? *Phys. Rev. Lett.* **126**, 041305 (2021).
- Liu, J., Cai, R. G. & Guo, Z. K. Large anisotropies of the stochastic gravitational wave background from cosmic domain walls. *Phys. Rev. Lett.* **126**, 141303 (2021).
- Alford, M. G. & Wilczek, F. Aharonov-Bohm interaction of cosmic strings with matter. *Phys. Rev. Lett.* 62, 1071–1074 (1989).
- Gerbert, P. D. Fermions in an Aharonov-Bohm field and cosmic strings. *Phys. Rev. D.* 40, 1346–1349 (1989).
- Yang, Y. S. Cosmic strings in a product Abelian gauge field theory. *Nucl. Phys. B* 885, 25–33 (2014).
- Wang, J. H., Ma, K. & Li, K. Influences of a topological defect on the spin Hall effect. *Phys. Rev. A* 87, 032107 (2013).
- Hu, J. Z. et al. Quantum simulation of Unruh radiation. Nat. Phys. 15, 785–789 (2019).
- de Nova, J. R. M. et al. Observation of thermal Hawking radiation and its temperature in an analogue black hole. *Nature* 569, 688–691 (2019).
- Philbin, T. G. et al. Fiber-optical analog of the event horizon. Science 319, 1367–1370 (2008).
- Belgiorno, F. et al. Hawking radiation from ultrashort laser pulse filaments. *Phys. Rev. Lett.* **105**, 203901 (2010).
- Drori, J. et al. Observation of stimulated hawking radiation in an optical analogue. *Phys. Rev. Lett.* **122**, 010404 (2019).
- Pendry, J. B., Schurig, D. & Smith, D. R. Controlling electromagnetic fields. Science 312, 1780–1782 (2006).
- 40. Leonhardt, U. Optical conformal mapping. Science 312, 1777–1780 (2006).
- Schurig, D. et al. Metamaterial electromagnetic cloak at microwave frequencies. *Science* **314**, 977–980 (2006).
- Li, J. S. & Pendry, J. B. Hiding under the carpet: a new strategy for cloaking. Phys. Rev. Lett. 101, 203901 (2008).
- 43. Chen, H. S. et al. Ray-optics cloaking devices for large objects in incoherent natural light. *Nat. Commun.* **4**, 2652 (2013).
- Narimanov, E. E. & Kildishev, A. V. Optical black hole: broadband omnidirectional light absorber. *Appl. Phys. Lett.* 95, 041106 (2009).
- Genov, D. A., Zhang, S. & Zhang, X. Mimicking celestial mechanics in metamaterials. *Nat. Phys.* 5, 687–692 (2009).
- Chen, H. Y., Miao, R. X. & Li, M. Transformation optics that mimics the system outside a Schwarzschild black hole. *Opt. Express* 18, 15183–15188 (2010).
- 47. Cheng, Q. et al. An omnidirectional electromagnetic absorber made of metamaterials. *N. J. Phys.* **12**, 063006 (2010).

- Sheng, C. et al. Trapping light by mimicking gravitational lensing. *Nat. Pho*tonics 7, 902–906 (2013).
- Lai, Y. et al. Illusion optics: the optical transformation of an object into another object. *Phys. Rev. Lett.* **102**, 253902 (2009).
- Sheng, C. et al. Definite photon deflections of topological defects in metasurfaces and symmetry-breaking phase transitions with material loss. *Nat. Commun.* 9, 4271 (2018).
- Sheng, C. et al. Wavefront shaping through emulated curved space in waveguide settings. *Nat. Commun.* 7, 10747 (2016).
- Batz, S. & Peschel, U. Linear and nonlinear optics in curved space. *Phys. Rev. A* 78, 043821 (2008).
- 53. Bekenstein, R. et al. Shape-preserving accelerating electromagnetic wave packets in curved space. *Phys. Rev. X* **4**, 011038 (2014).
- 54. Grier, D. G. A revolution in optical manipulation. Nature 424, 810-816 (2003).
- Wang, J. Advances in communications using optical vortices. *Photonics Res.* 4, B14–B28 (2016).
- Fickler, R. et al. Quantum entanglement of high angular momenta. *Science* 338, 640–643 (2012).
- Heckenberg, N. R. et al. Generation of optical phase singularities by computergenerated holograms. *Opt. Lett.* 17, 221–223 (1992).
- Marrucci, L., Manzo, C. & Paparo, D. Optical spin-to-orbital angular momentum conversion in inhomogeneous anisotropic media. *Phys. Rev. Lett.* **96**, 163905 (2006).
- Cai, X. L. et al. Integrated compact optical vortex beam emitters. *Science* 338, 363–366 (2012).
- Yu, N. F. et al. Light propagation with phase discontinuities: generalized laws of reflection and refraction. *Science* **334**, 333–337 (2011).
- 61. Chen, Y. et al. Vector vortex beam emitter embedded in a photonic chip. *Phys. Rev. Lett.* **124**, 153601 (2020).
- 62. Chen, Y. et al. Mapping twisted light into and out of a photonic chip. *Phys. Rev. Lett.* **121**, 233602 (2018).
- 63. Wang, Q. et al. Vortex states in an acoustic Weyl crystal with a topological lattice defect. *Nat. Commun.* **12**, 3654 (2021).
- Pollock, M. D. On the Dirac equation in curved space-time. Acta Phys. Polonica B 41, 1827–1846 (2010).
- Collas, P. & Klein, D. The Dirac Equation in Curved Spacetime: A Guide for Calculations. (Cham: Springer, 2019).
- Oliva-Leyva, M. & Naumis, G. G. Effective Dirac Hamiltonian for anisotropic honeycomb lattices: optical properties. *Phys. Rev. B* 93, 035439 (2016).
- 67. Pfeiffer, P. et al. Ouantum memristors. *Sci. Rep.* **6**. 29507 (2016).
- Gao, J. et al. Quantum Advantage timestamp membosonsampling Preprint at https://doi.org/10.48550/arXiv.2012.03967 (2020).